

# A Minimal Supersymmetric Cosmological Model

Ewan Stewart

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Beyond the Standard Models of  
Particle Physics, Cosmology and Astrophysics  
2 February 2010  
Cape Town, South Africa

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Gary N Felder, Hyunbyuk Kim, Wan-Il Park, EDS	hep-ph/0703275
Richard Easter, John T Giblin, Eugene A Lim, Wan-Il Park, EDS	arXiv:0801.4197
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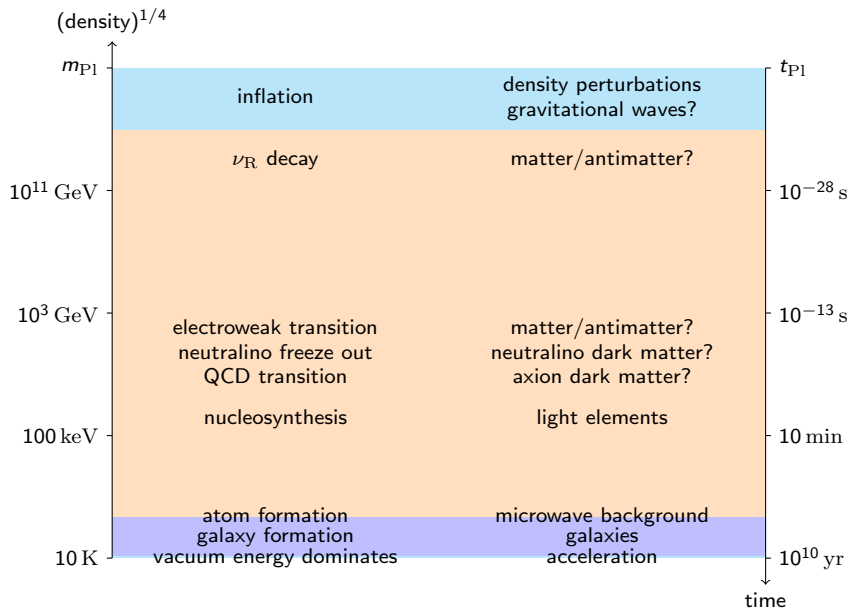
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# Standard model of cosmology



## Moduli and gravitinos

Moduli are cosmologically dangerous. Nucleosynthesis constrains

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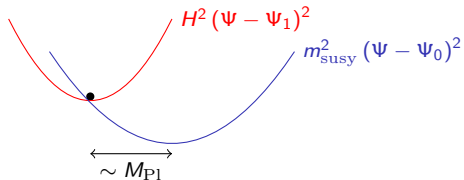


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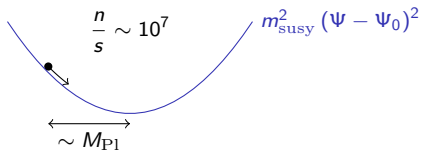


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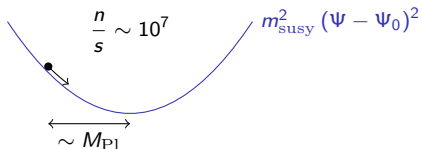


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Moduli generated:  $H \lesssim m_{\text{susy}}$

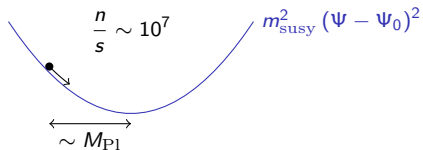


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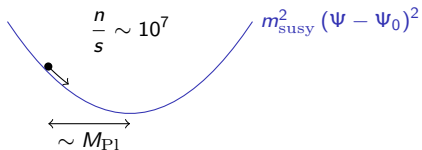
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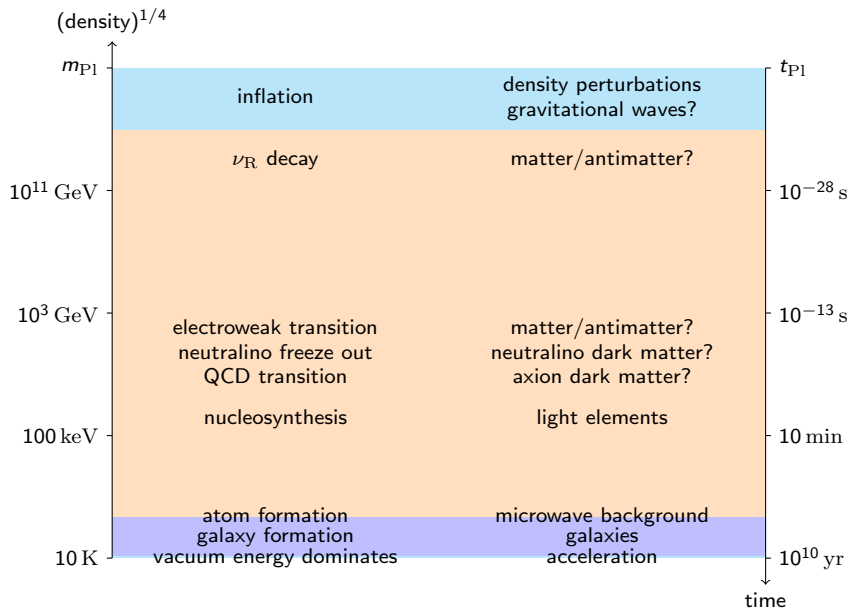


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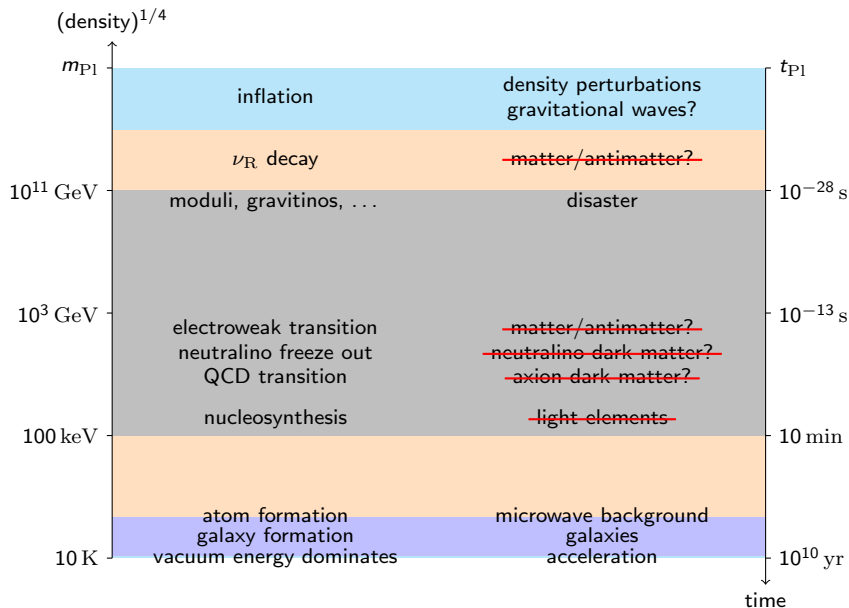
after

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# Standard model of cosmology



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# Minimal Supersymmetric Standard Model

$$W = \lambda_u QH_u \bar{u} + \lambda_d QH_d \bar{d} + \lambda_e LH_d \bar{e} + \mu H_u H_d$$

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But

▶  $\mu?$

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- ▶ neutrino masses?
- ▶ strong  $CP$ ?



# Minimal Supersymmetric Cosmological Model

$$W = \lambda_u QH_u\bar{u} + \lambda_d QH_d\bar{d} + \lambda_e LH_d\bar{e} + \frac{1}{2}\lambda_\nu (LH_u)^2 + \lambda_\mu \phi^2 H_u H_d + \lambda_\chi \phi \chi \bar{\chi}$$

# Minimal Supersymmetric Cosmological Model

MSSM

$$W = \lambda_u QH_u \bar{u} + \lambda_d QH_d \bar{d} + \lambda_e LH_d \bar{e} + \frac{1}{2} \lambda_\nu (LH_u)^2 + \lambda_\mu \phi^2 H_u H_d + \lambda_\chi \phi \chi \bar{\chi}$$

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# Minimal Supersymmetric Cosmological Model

MSSM

neutrino masses

MSSM  $\mu$ -term

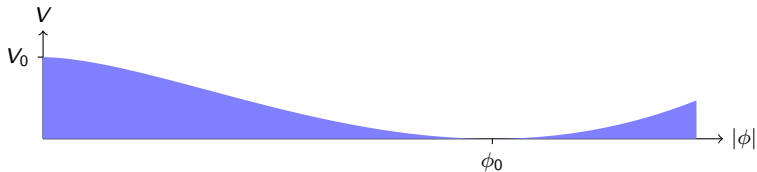
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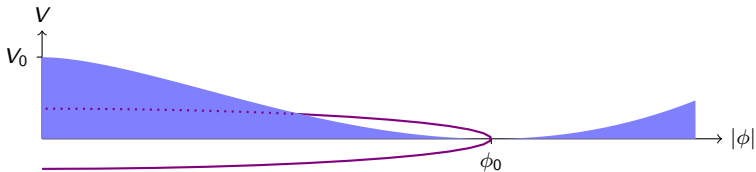
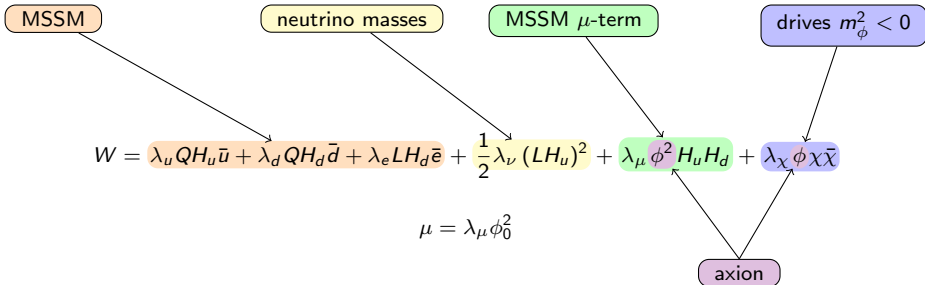
# Minimal Supersymmetric Cosmological Model

MSSM      neutrino masses      MSSM  $\mu$ -term      drives  $m_\phi^2 < 0$

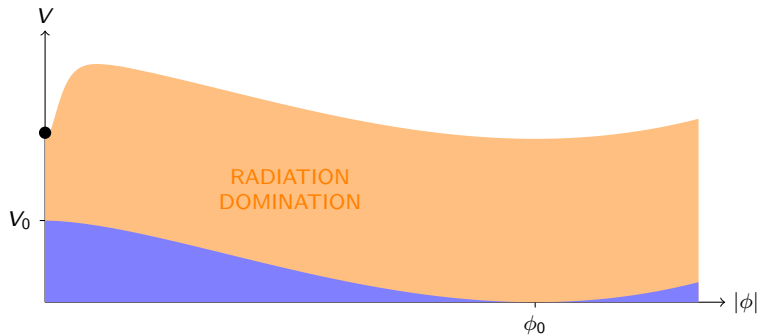
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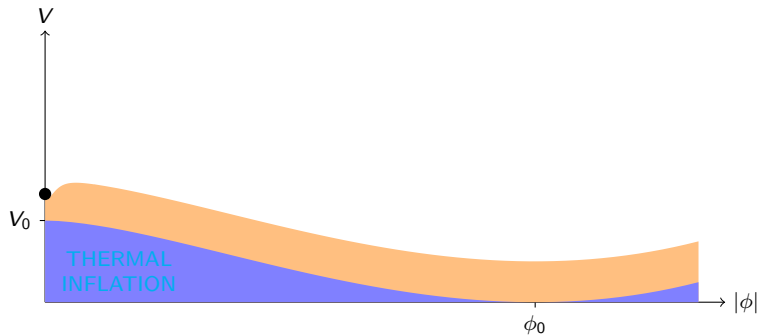
# Minimal Supersymmetric Cosmological Model



# Thermal inflation

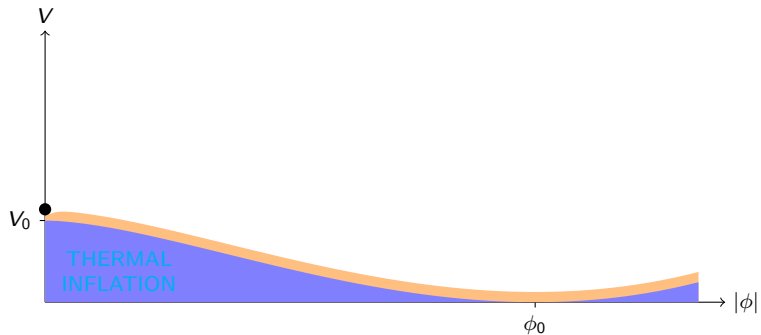


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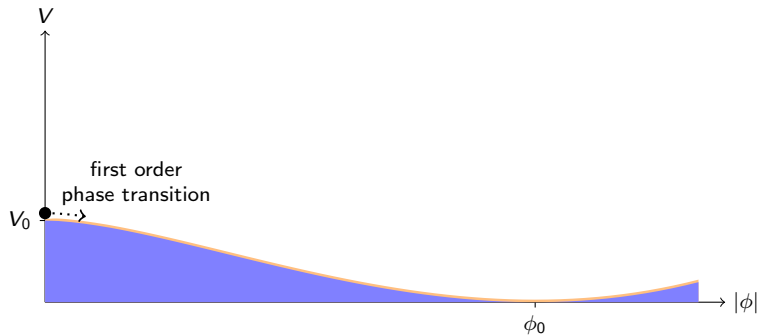




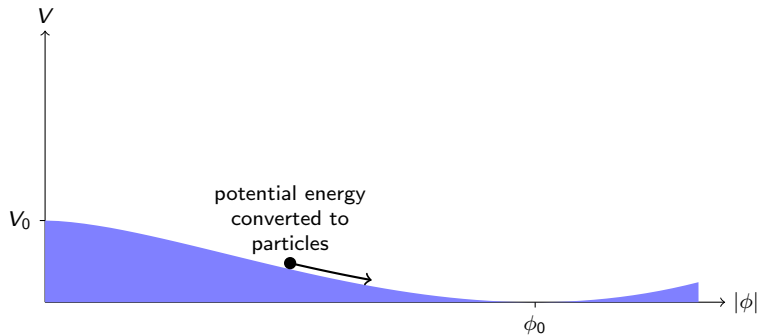
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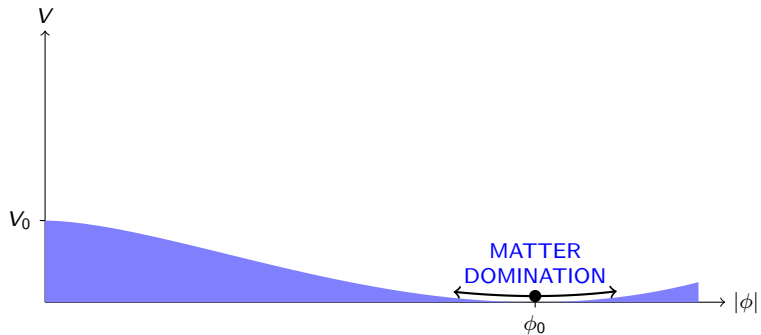
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## Key properties of thermal inflation

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$$\phi_0 \sim 10^{10} \text{ to } 10^{12} \text{ GeV}$$

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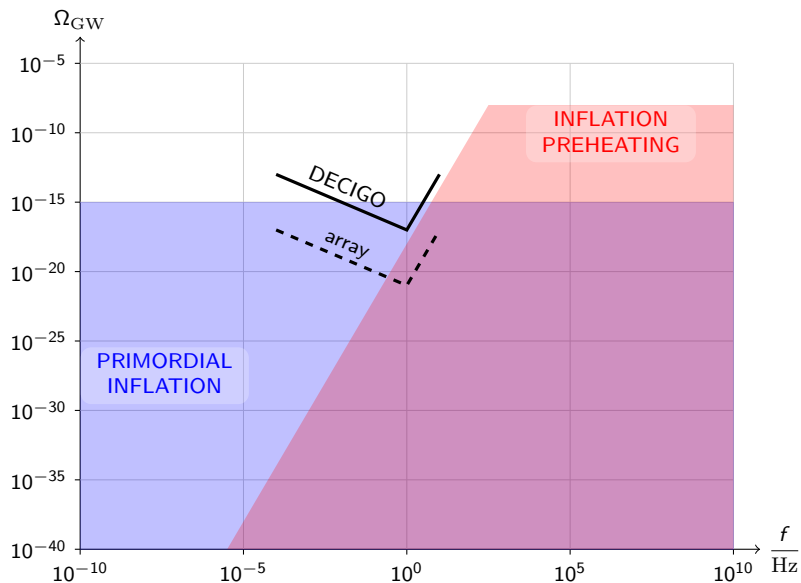
$$N \sim 10 \implies \begin{array}{l} \text{primordial perturbations} \\ \text{from slow-roll inflation} \\ \text{preserved on large scales} \end{array}$$

Low energy scale

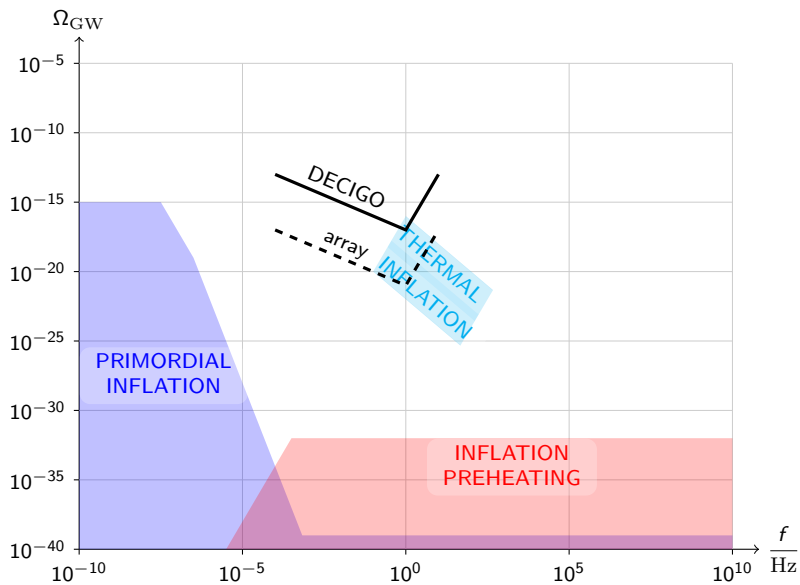
$$V_0^{1/4} \sim 10^6 \text{ to } 10^7 \text{ GeV} \implies \text{moduli regenerated with sufficiently small abundance}$$



# Gravitational waves



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# Baryogenesis

Key assumption

$$m_{LH_u}^2 = \frac{1}{2} (m_L^2 + m_{H_u}^2) < 0$$

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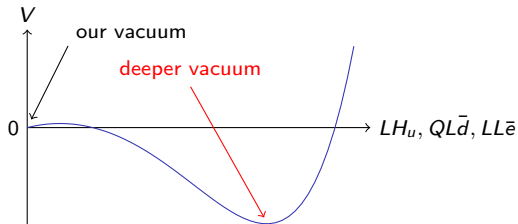
Implies a dangerous **non-MSSM vacuum** with

$$LH_u \sim (10^9 \text{ GeV})^2$$

and

$$\lambda_d QL\bar{d} + \lambda_e LL\bar{e} = \mu LH_u$$

eliminating the  $\mu$ -term contribution to  $LH_u$ 's mass squared.



## Reduction

$$W = \lambda_u QH_u \bar{u} + \lambda_d QH_d \bar{d} + \lambda_e LH_d \bar{e} + \frac{1}{2} \lambda_\nu (LH_u)^2 + \lambda_\mu \phi^2 H_u H_d + \lambda_\chi \phi \chi \bar{\chi}$$

## Reduction

$$W = \lambda_u Q H_u \bar{u} + \lambda_d Q H_d \bar{d} + \lambda_e L H_d \bar{e} + \frac{1}{2} \lambda_\nu (L H_u)^2 + \lambda_\mu \phi^2 H_u H_d + \lambda_\chi \phi \chi \bar{\chi}$$

$$L = \begin{pmatrix} 1 \\ 0 \end{pmatrix}, \quad H_u = \begin{pmatrix} 0 \\ h_u \end{pmatrix}, \quad H_d = \begin{pmatrix} h_d \\ 0 \end{pmatrix}, \quad \bar{e} = (0)$$

$$\bar{u} = (0 \ 0 \ 0), \quad Q = \begin{pmatrix} 0 & 0 & 0 \\ d/\sqrt{2} & 0 & 0 \end{pmatrix}, \quad \bar{d} = (d/\sqrt{2} \ 0 \ 0)$$

$$\phi = \phi, \quad \chi = 0, \quad \bar{\chi} = 0$$

# Potential

$$\begin{aligned} V = & V_0 + m_L^2 |l|^2 - m_{H_u}^2 |h_u|^2 + m_{H_d}^2 |h_d|^2 - m_\phi^2 |\phi|^2 \\ & + \frac{1}{2} (m_Q^2 + m_d^2) |d|^2 + \frac{1}{2} (m_L^2 + m_e^2) |e|^2 \\ & + \left[ \frac{1}{2} A_\nu \lambda_\nu l^2 h_u^2 - A_\mu \lambda_\mu \phi^2 h_u h_d - \frac{1}{2} A_d \lambda_d h_d d^2 + \frac{1}{2} A_e \lambda_e h_d e^2 + \text{c.c.} \right] \\ & + |\lambda_\nu l h_u^2|^2 + |\lambda_\nu l^2 h_u - \lambda_\mu \phi^2 h_d|^2 + \left| \lambda_\mu \phi^2 h_u + \frac{1}{2} \lambda_d d^2 + \frac{1}{2} \lambda_e e^2 \right|^2 \\ & + |\lambda_d h_d d|^2 + |\lambda_e h_d e|^2 + |2\lambda_\mu \phi h_u h_d|^2 \\ & + \frac{1}{2} g^2 \left( |h_u|^2 - |h_d|^2 - |l|^2 + \frac{1}{2} |d|^2 + \frac{1}{2} |e|^2 \right)^2 \end{aligned}$$

# Potential

drives thermal inflation

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$h_u$  rolls away

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$h_u$  stabilized with fixed phase

$$+ \left[ \frac{1}{2} A_\nu \lambda_\nu l^2 h_u^2 - A_\mu \lambda_\mu \phi^2 h_u h_d - \frac{1}{2} A_d \lambda_d h_d d^2 + \frac{1}{2} A_e \lambda_e h_d e^2 + \text{c.c.} \right] \\ + \left| \lambda_\nu l h_u^2 \right|^2 + \left| \lambda_\nu l^2 h_u - \lambda_\mu \phi^2 h_d \right|^2 + \left| \lambda_\mu \phi^2 h_u + \frac{1}{2} \lambda_d d^2 + \frac{1}{2} \lambda_e e^2 \right|^2 \\ + |\lambda_d h_d d|^2 + |\lambda_e h_d e|^2 + |2\lambda_\mu \phi h_u h_d|^2 \\ + \frac{1}{2} g^2 \left( |h_u|^2 - |h_d|^2 - |l|^2 + \frac{1}{2} |d|^2 + \frac{1}{2} |e|^2 \right)^2$$

# Potential

drives thermal inflation

$lh_u$  rolls away

$\phi$  rolls away

$$V = V_0 + m_L^2 |l|^2 - m_{H_u}^2 |h_u|^2 + m_{H_d}^2 |h_d|^2 - m_\phi^2 |\phi|^2$$

$$+ \frac{1}{2} (m_Q^2 + m_d^2) |d|^2 + \frac{1}{2} (m_L^2 + m_e^2) |e|^2$$

$lh_u$  stabilized with fixed phase

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drives thermal inflation

$h_u$  rolls away

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$$V = V_0 + m_L^2 |l|^2 - m_{H_u}^2 |h_u|^2 + m_{H_d}^2 |h_d|^2 - m_\phi^2 |\phi|^2$$

$$+ \frac{1}{2} (m_Q^2 + m_d^2) |d|^2 + \frac{1}{2} (m_L^2 + m_e^2) |e|^2$$

$h_d$  forced out

$h_u$  stabilized with fixed phase

$$+ \left[ \frac{1}{2} A_\nu \lambda_\nu l^2 h_u^2 - A_\mu \lambda_\mu \phi^2 h_u h_d - \frac{1}{2} A_d \lambda_d h_d d^2 + \frac{1}{2} A_e \lambda_e h_d e^2 + \text{c.c.} \right]$$

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$lh_u$  rolls away

$\phi$  rolls away

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~~$$+ \frac{1}{2} (m_Q^2 + m_d^2) |d|^2 + \frac{1}{2} (m_L^2 + m_e^2) |e|^2$$~~

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~~$$+ \left[ \frac{1}{2} A_\nu \lambda_\nu l^2 h_u^2 - A_\mu \lambda_\mu \phi^2 h_u h_d - \frac{1}{2} A_d \lambda_d h_d d^2 + \frac{1}{2} A_e \lambda_e h_d e^2 + \text{c.c.} \right]$$~~

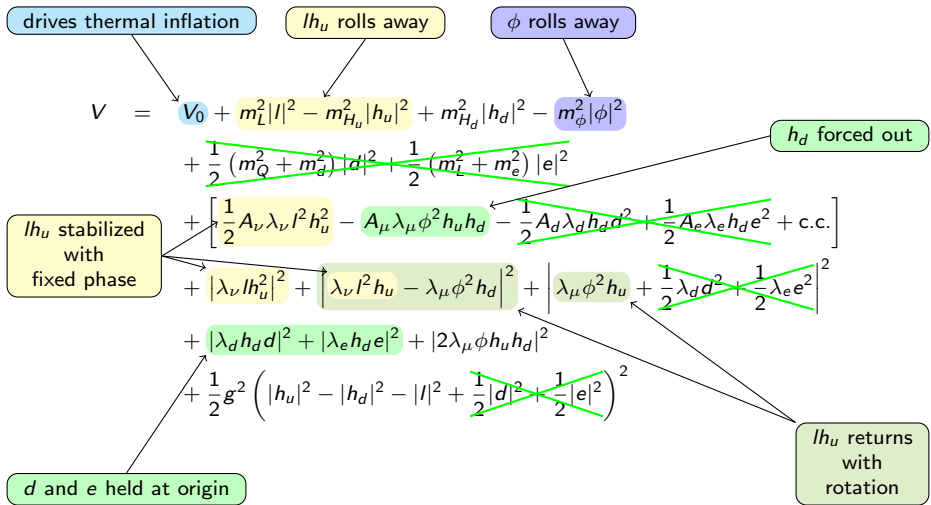
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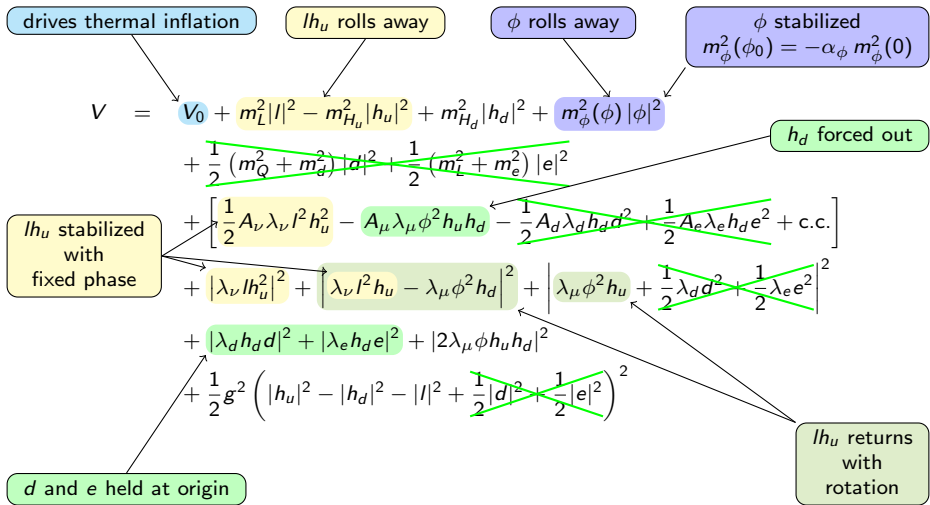
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$d$  and  $e$  held at origin

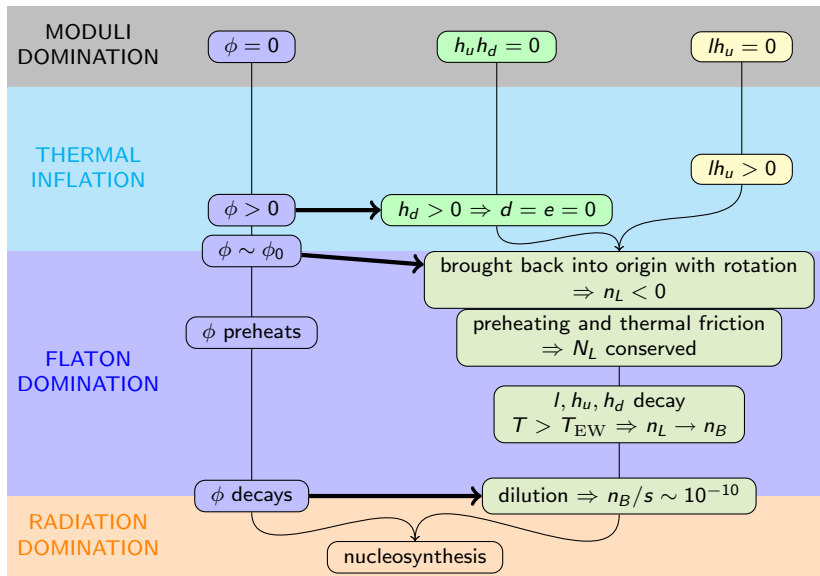
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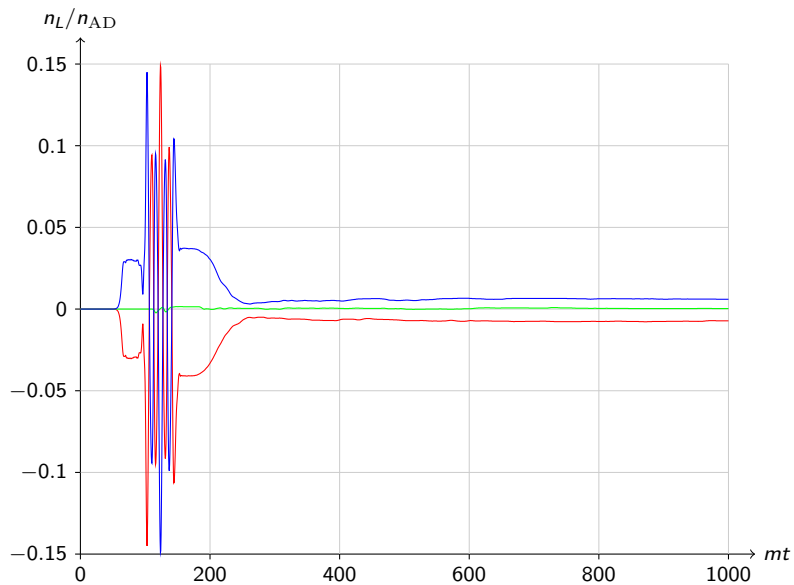


# Baryogenesis





## Numerical simulation



## Baryon asymmetry

$$\frac{n_B}{s} \sim \frac{n_L}{n_{AD}} \frac{n_{AD}}{n_\phi} \frac{T_d}{m_\phi(\phi_0)}$$

## Baryon asymmetry

$$\frac{n_B}{s} \sim \frac{n_L}{n_{AD}} \frac{n_{AD}}{n_\phi} \frac{T_d}{m_\phi(\phi_0)}$$

Using

$$n_\phi \sim m_\phi(\phi_0) \phi_0^2 \quad , \quad m_\phi^2(\phi_0) \sim \alpha_\phi m_\phi^2(0) \quad , \quad n_{AD} \sim m_{LH_u} l_0^2$$

$$l_0 \sim 10^9 \text{ GeV} \sqrt{\left(\frac{10^{-2} \text{ eV}}{m_\nu}\right) \left(\frac{m_{LH_u}}{10^3 \text{ GeV}}\right)}$$

and

$$T_d \sim 1 \text{ GeV} \left(\frac{10^{12} \text{ GeV}}{\phi_0}\right) \left(\frac{|\mu|}{10^3 \text{ GeV}}\right)^2$$

gives

$$\frac{n_B}{s} \sim 10^{-10} \left(\frac{n_L/n_{AD}}{10^{-2}}\right) \left(\frac{10^{12} \text{ GeV}}{\phi_0}\right)^3 \left(\frac{10^{-2} \text{ eV}}{m_\nu}\right) \left(\frac{|\mu|}{10^3 \text{ GeV}}\right)^2 \left(\frac{10^{-1}}{\alpha_\phi}\right) \left(\frac{m_{LH_u}}{m_\phi(0)}\right)^2$$

## Baryon asymmetry

$$\frac{n_B}{s} \sim \frac{n_L}{n_{AD}} \frac{n_{AD}}{n_\phi} \frac{T_d}{m_\phi(\phi_0)}$$

Using

$$n_\phi \sim m_\phi(\phi_0) \phi_0^2 \quad , \quad m_\phi^2(\phi_0) \sim \alpha_\phi m_\phi^2(0) \quad , \quad n_{AD} \sim m_{LH_u} l_0^2$$

$$l_0 \sim 10^9 \text{ GeV} \sqrt{\left(\frac{10^{-2} \text{ eV}}{m_\nu}\right) \left(\frac{m_{LH_u}}{10^3 \text{ GeV}}\right)}$$

and

$$T_d \sim 1 \text{ GeV} \left(\frac{10^{12} \text{ GeV}}{\phi_0}\right) \left(\frac{|\mu|}{10^3 \text{ GeV}}\right)^2$$

gives

$$\frac{n_B}{s} \sim 10^{-10} \left(\frac{n_L/n_{AD}}{10^{-2}}\right) \left(\frac{10^{12} \text{ GeV}}{\phi_0}\right)^3 \left(\frac{10^{-2} \text{ eV}}{m_\nu}\right) \left(\frac{|\mu|}{10^3 \text{ GeV}}\right)^2 \left(\frac{10^{-1}}{\alpha_\phi}\right) \left(\frac{m_{LH_u}}{m_\phi(0)}\right)^2$$

which suggests

$$\phi_0 \sim 10^{12} \text{ GeV}$$

# Dark matter candidates

Peccei-Quinn symmetry

$$W = \lambda_u QH_u \bar{u} + \lambda_d QH_d \bar{d} + \lambda_e LH_d \bar{e} + \frac{1}{2} \lambda_\nu (LH_u)^2 + \lambda_\mu \phi^2 H_u H_d + \lambda_\chi \phi \chi \bar{\chi}$$

# Dark matter candidates

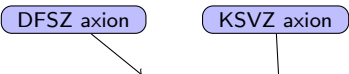
Peccei-Quinn symmetry

DFSZ axion

$$W = \lambda_u QH_u \bar{u} + \lambda_d QH_d \bar{d} + \lambda_e LH_d \bar{e} + \frac{1}{2} \lambda_\nu (LH_u)^2 + \lambda_\mu \phi^2 H_u H_d + \lambda_\chi \phi \chi \bar{\chi}$$

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DFSZ axion                      KSVZ axion

(Arrows point from DFSZ axion to  $\lambda_\mu \phi^2 H_u H_d$  and from KSVZ axion to  $\lambda_\chi \phi \chi \bar{\chi}$ )

Axion

$$m_a \sim \frac{\Lambda_{\text{QCD}}^2}{f_a} \quad \text{where } f_a = \frac{\sqrt{2} \phi_0}{N}$$
$$\simeq 6.2 \times 10^{-6} \text{ eV} \left( \frac{10^{12} \text{ GeV}}{f_a} \right)$$



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Peccei-Quinn symmetry

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↘    ↘

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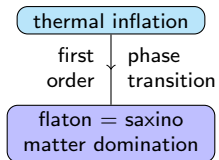
Axino

$$m_{\tilde{a}} = \frac{1}{16\pi^2} \sum_{\chi} \lambda_{\chi}^2 A_{\chi}$$
$$\sim 1 \text{ to } 10 \text{ GeV}$$

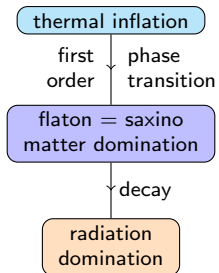
# Dark matter genesis

thermal inflation

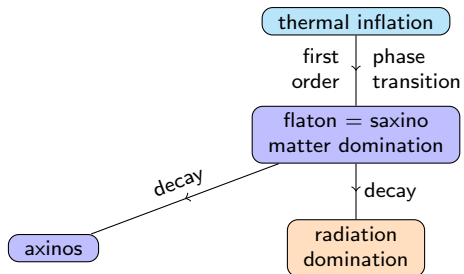
# Dark matter genesis



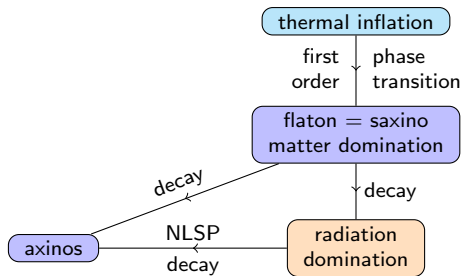
# Dark matter genesis



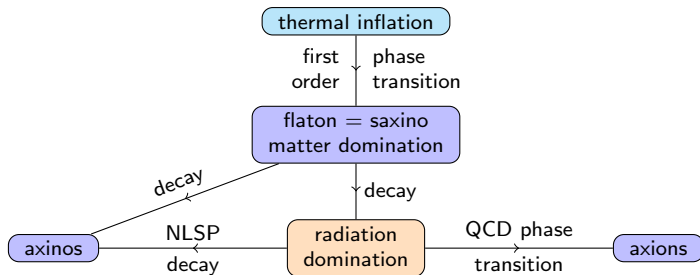
# Dark matter genesis



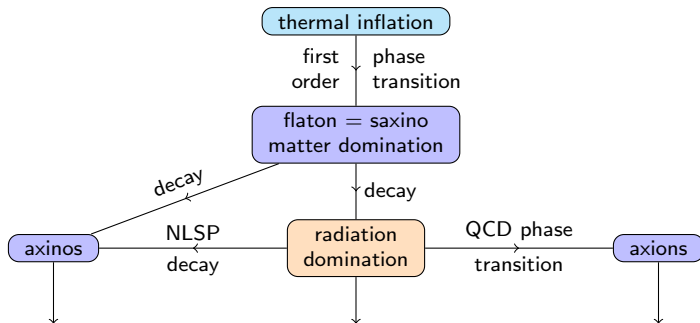
# Dark matter genesis



# Dark matter genesis



# Dark matter genesis





# Dark matter abundance

Axion

Axino

# Dark matter abundance

## Axion Misalignment

$$\Omega_a \sim 3 \left( \frac{f_a}{10^{12} \text{ GeV}} \right)^{1.2}$$

## Axino

# Dark matter abundance

## Axion Misalignment

$$\Omega_a \sim 3 \left( \frac{f_a}{10^{12} \text{ GeV}} \right)^{1.2}$$

## Axino Flaton decay

$$\Omega_{\tilde{a}} \simeq 0.04 \left( \frac{\alpha_{\tilde{a}}}{10^{-1}} \right)^2 \left( \frac{m_{\tilde{a}}}{1 \text{ GeV}} \right)^3 \left( \frac{10^{12} \text{ GeV}}{\phi_0} \right)^2 \left( \frac{1 \text{ GeV}}{T_d} \right)$$

# Dark matter abundance

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## Thermal NLSP decay

$$\Omega_{\tilde{a}} \sim 10 \left( \frac{m_{\tilde{a}}}{1 \text{ GeV}} \right) \left( \frac{10^{12} \text{ GeV}}{\phi_0} \right)^2$$

## Dark matter abundance

Flaton decays late

$$T_d \sim 1 \text{ GeV} \left( \frac{|\mu|}{10^3 \text{ GeV}} \right)^2 \left( \frac{10^{12} \text{ GeV}}{\phi_0} \right)$$

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Axion Misalignment

$$\Omega_a \sim 3 \left( \frac{f_a}{10^{12} \text{ GeV}} \right)^{1.2} \times \begin{cases} 1 & \text{for } T_d \gg 1 \text{ GeV} \\ \left( \frac{T_d}{1 \text{ GeV}} \right)^2 & \text{for } T_d \ll 1 \text{ GeV} \end{cases}$$

Axino Flaton decay

$$\Omega_{\tilde{a}} \simeq 0.04 \left( \frac{\alpha_{\tilde{a}}}{10^{-1}} \right)^2 \left( \frac{m_{\tilde{a}}}{1 \text{ GeV}} \right)^3 \left( \frac{10^{12} \text{ GeV}}{\phi_0} \right)^2 \left( \frac{1 \text{ GeV}}{T_d} \right)$$

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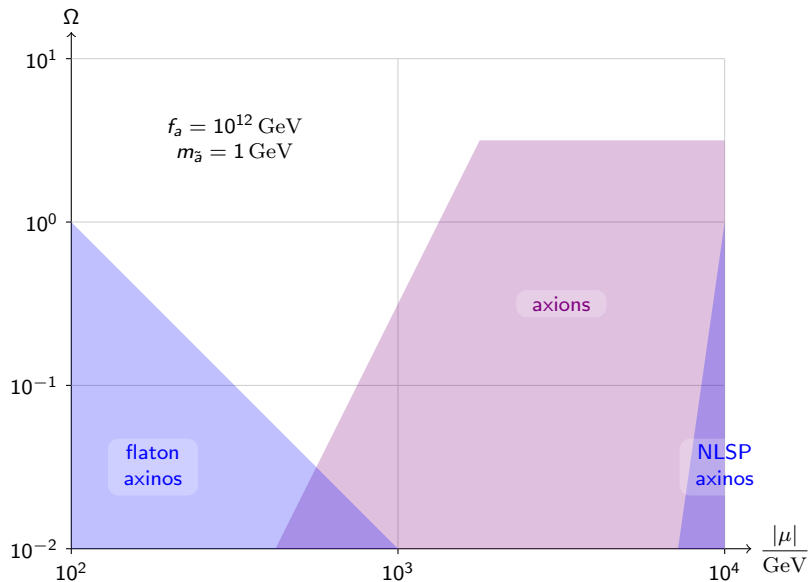
Axino Flaton decay

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Thermal NLSP decay

$$\Omega_{\tilde{a}} \sim 10 \left( \frac{m_{\tilde{a}}}{1 \text{ GeV}} \right) \left( \frac{10^{12} \text{ GeV}}{\phi_0} \right)^2 \times \begin{cases} 1 & \text{for } T_d \gg \frac{m_N}{7} \\ \left( \frac{7T_d}{m_N} \right)^7 & \text{for } T_d \ll \frac{m_N}{7} \end{cases}$$

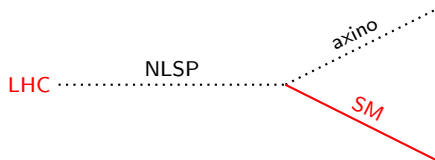
# Dark matter composition





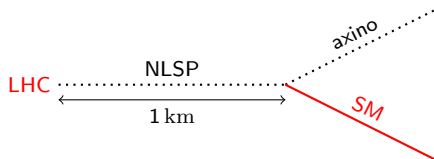
## Axino LHC signal

NLSPs produced by the LHC decay to axinos plus Standard Model particles



## Axino LHC signal

NLSPs produced by the LHC decay to axinos plus Standard Model particles



with a decay length

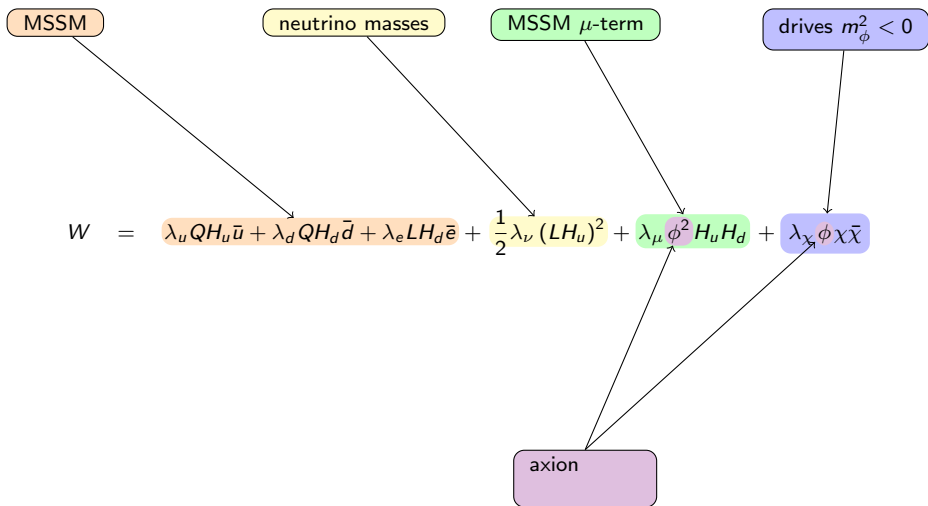
$$\frac{1}{\Gamma_{N \rightarrow \tilde{a}}} \sim \frac{16\pi\phi_0^2}{m_N^3} \sim 1 \text{ km} \left( \frac{200 \text{ GeV}}{m_N} \right)^3 \left( \frac{\phi_0}{10^{12} \text{ GeV}} \right)^2$$

and well constrained parameters

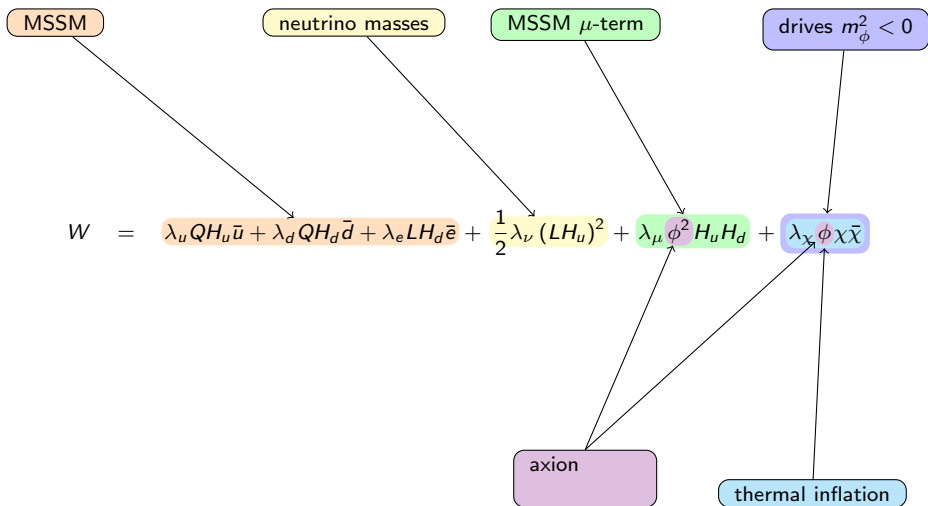
$$\phi_0 \sim 10^{12} \text{ GeV}$$

$$m_{\tilde{a}} \simeq 1 \text{ GeV}$$

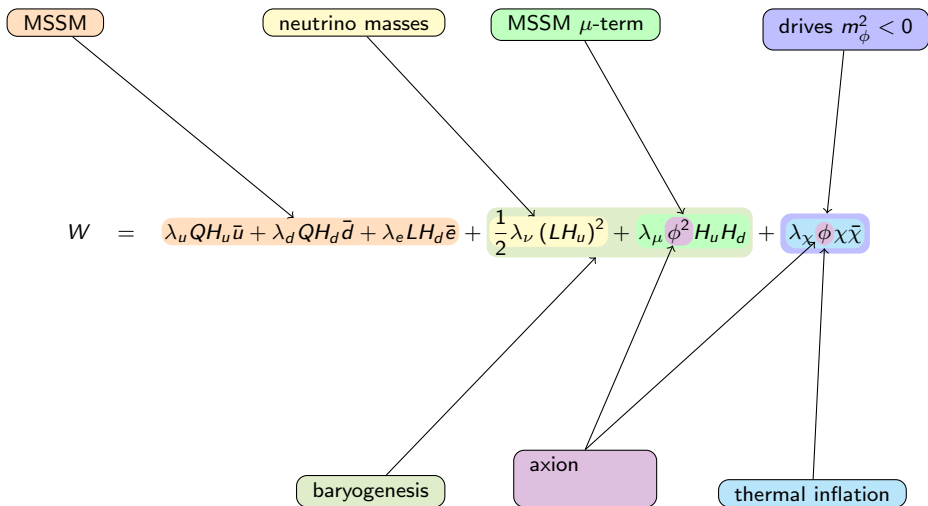
# Simple model



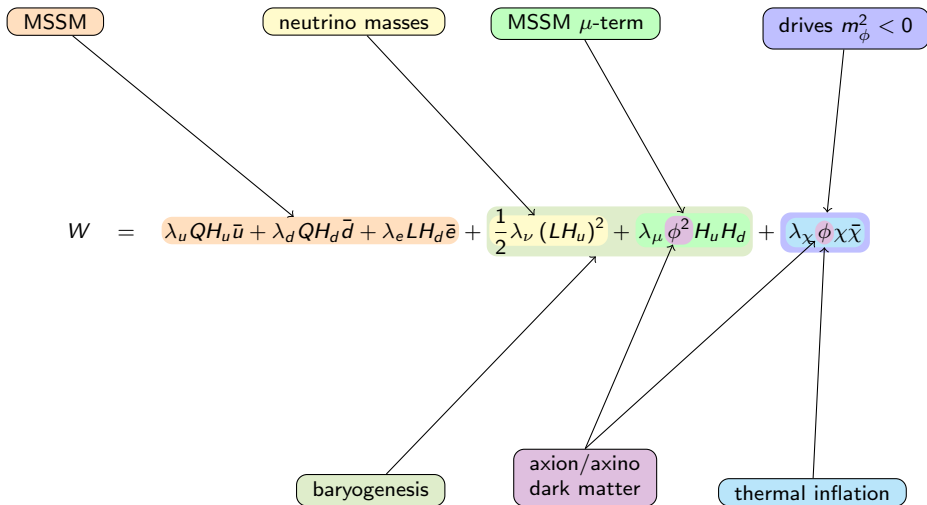
# Simple model



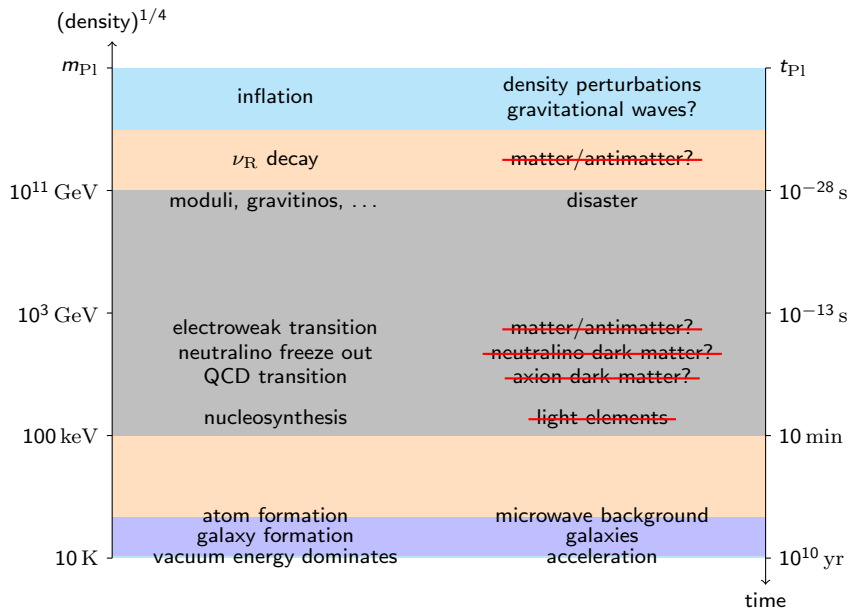
# Simple model



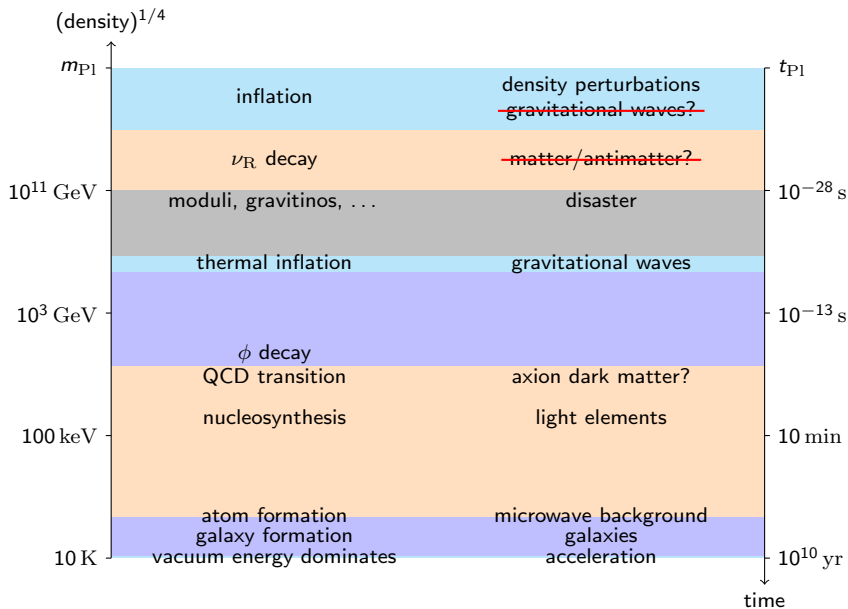
# Simple model



# Rich cosmology

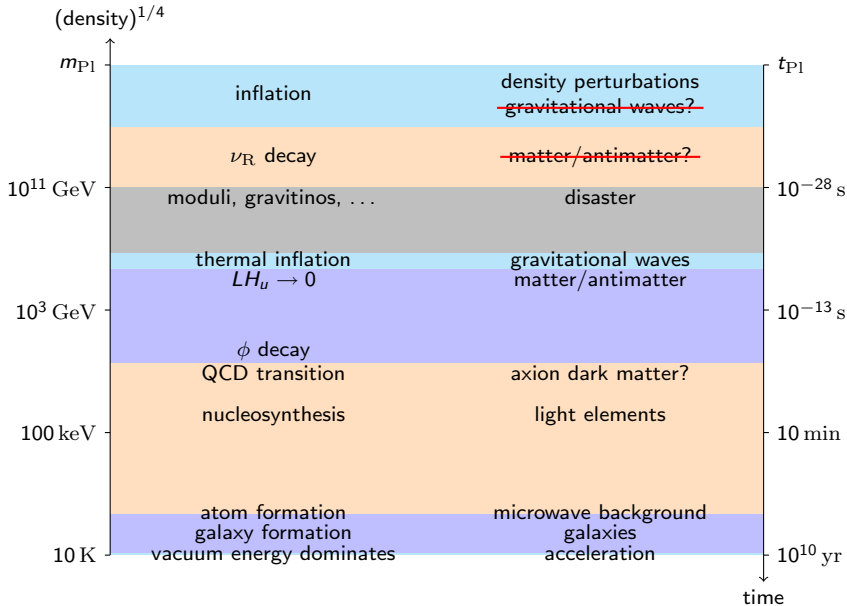


# Rich cosmology

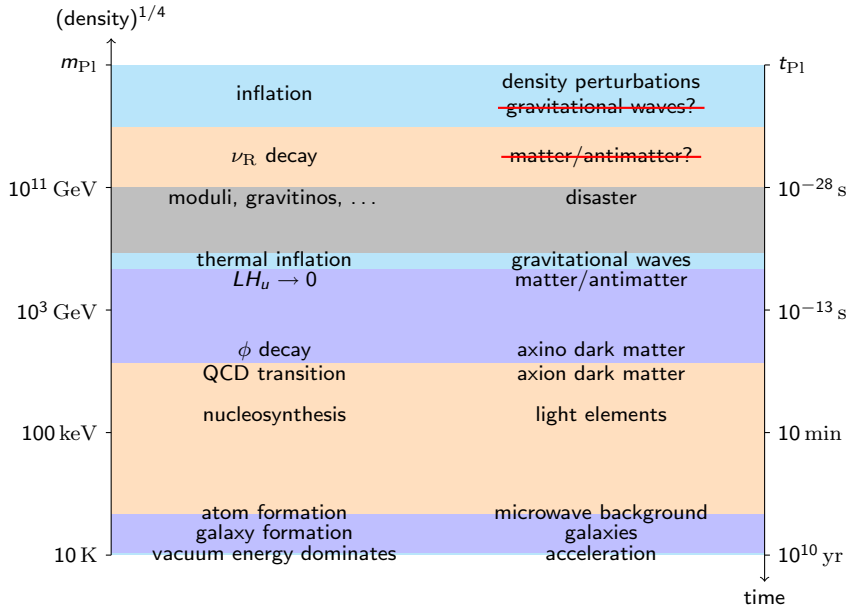




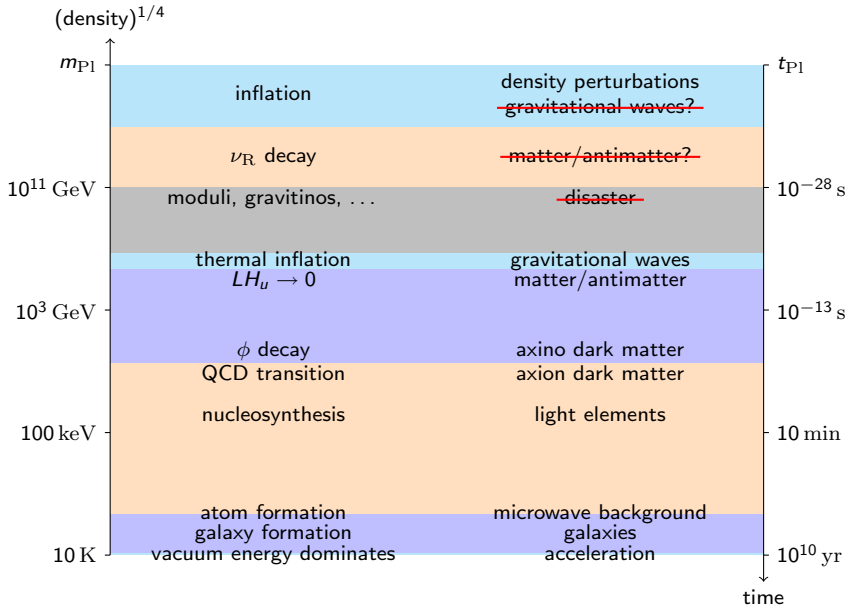
# Rich cosmology



# Rich cosmology



# Rich cosmology



# A Minimal Supersymmetric Cosmological Model

## Introduction

- Standard model of cosmology
- Moduli and gravitinos

## A Minimal Supersymmetric Cosmological Model

- MSSM
- MSCM
- Thermal inflation
- Baryogenesis
- Dark matter

## Summary

- Simple model
- Rich cosmology