Homework 4

Optional extra question.

Q4.3. Let $f(z, z^*)$ be a complex function and f be the vector field on the complex plane with Cartesian components (Re f, Im f). Show that

$$\int_{\partial A} f \, dz^* = \int_A \left(\boldsymbol{\nabla} \wedge \boldsymbol{f} - i \boldsymbol{\nabla} \cdot \boldsymbol{f} \right) dA \qquad (Q4.3.1)$$

where ∂A is the boundary of the area A in the complex plane. Interpret

$$f = \frac{1}{2\pi z^*}$$
(Q4.3.2)

in terms of two dimensional electromagnetism.